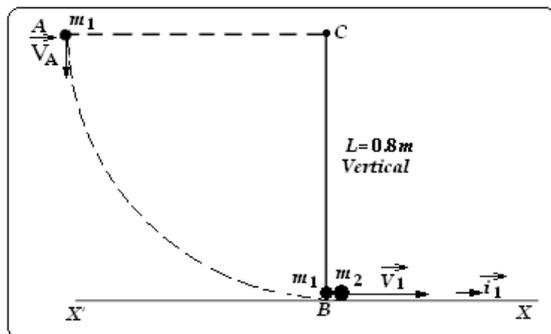


### MID YEAR EXAM

Answer the following questions:

**I- Conservation and non conservation of mechanical energy- collision** .....(7 pts.)

Consider two point masses  $m_1 = 0.1\text{Kg}$  and  $m_2 = 0.4\text{Kg}$ . The point mass  $m_1$  is fixed to one end "A" of a mass less, inextensible string CA, whose other end is tied to a fixed support C. The length of the string is  $L = 0.8\text{m}$ . The point mass  $m_2$  rests on a horizontal surface  $x'x$ , taken as zero reference G.P.E.



$m_1$  taken to position "A" of same level as C, and with  $CA=L$ ,  $m_1$  is given a vertical downward velocity  $\vec{V}_A$ , thus  $m_1$  reaches B with a velocity  $\vec{V}_1$ , of magnitude  $V_1 = 5\text{m/s}$ . ( $\vec{V}_1 = 5\vec{i}$ )  $m_1$  enters into head on collision with  $m_2$ , which is originally at rest.

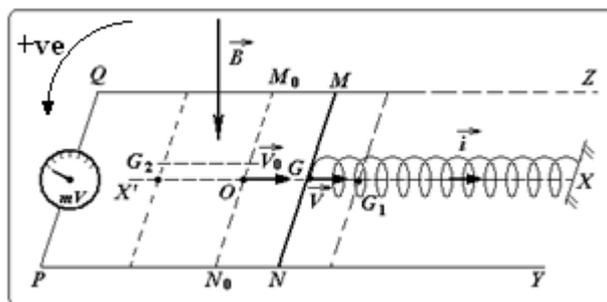
Just after collision  $m_2$  moves with velocity  $\vec{V}_2'$ , of magnitude  $2\text{m/s}$ , ( $\vec{V}_2' = 2\vec{i}$ ) and  $m_1$  moves with velocity  $\vec{V}_1'$ . Neglect air resistance. Use  $g = 10\text{m/s}^2$ .

- 1- Explain why the mechanical energy of the system ( $m_1$ , earth) along the path  $\widehat{AB}$  is conserved, then determine its value, and deduce the magnitude of  $\vec{V}_A$ .
- 2- Determine  $\vec{V}_1'$ . Is the collision between  $m_1$  and  $m_2$  perfectly elastic? Why?
- 3- In what direction and with what maximum angle would the string CB deviate after collision.
- 4- After collision,  $m_2$  starts with the speed  $2\text{m/s}$ , and stops on the horizontal surface  $x'x$  along a distance of  $5\text{m}$ , due to friction force  $\vec{f}$  supposed constant.
  - a) Find  $f$ .
  - b) Determine G.P.E, M.E, and K.E of  $m_2$  in terms of  $x$ . Where  $x$  represents the position of  $m_2$  with origin B. Draw the graphs representing G.P.E, M.E, and K.E versus  $x$ .

**II- Horizontal Elastic pendulum - Electromagnetic induction**.....(7 pts.)

In the figure: the horizontal spring is mass less, of stiffness  $K = 50\text{N/m}$ . The rod MN is uniform, homogeneous, of mass  $0.5\text{Kg}$ , and length  $L = 0.25\text{m}$ .

One end of the spring is fixed; the other end holds MN through its center G. The rod MN is a conductor free to slide on the horizontal wires QZ and PY, with MN perpendicular to them. The millivoltmeter has very high resistance. The whole circuit MNPQ lies in a horizontal plane. The rod MN, the rails QZ, PY, and all connecting wires are of negligible resistance. QZ and PY are parallel, to the axis  $x'x$  of the spring, QZ is the internal wire.



At  $t_0 = 0$ , the spring has its free length, the rod is at position  $M_0N_0$  is given a velocity  $\vec{V}_0(\text{m/s}) = 2\vec{i}$ .  $\vec{i}$  is a unit vector along  $x'ox$ . The zero reference G.P.E is level of  $x'x$ . At any  $t$ ,  $\vec{OG} = x$  and  $\vec{V} = x'\vec{i}$ . friction is negligible.

- 1- Write the expression of the M.E of the system (rod MN, spring).
- 2- Using the principle of conservation of M.E, determine the differential equation of motion for G, then deduce the proper angular frequency  $\omega_0$  and proper period  $T_0$  of this elastic pendulum.
- 3- Determine the time equation of motion of G.  $x = ?$  in terms of t.
- 4- The whole circuit is subjected to a uniform magnetic field  $\vec{B}$ , vertically downward, of magnitude 0.4T.

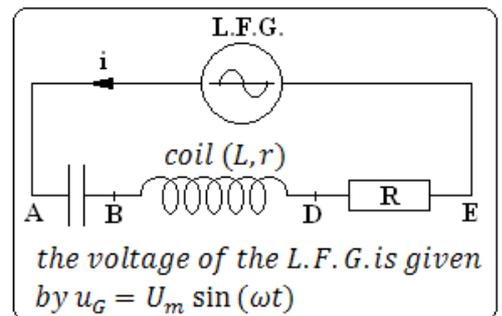
Denote by  $S_0$  the surface area  $M_0N_0PQ$ , and by  $S$  the surface area of  $MNPQ$ .

- a) Determine the area of  $MNN_0M_0$  or  $\Delta S$  in terms of  $x$ , then deduce the magnetic flux  $\Phi$  in terms of  $S_0$  and  $x$ .
- b) Determine the induced e.m.f across MN in terms of  $V$ , and calculate its value  $e_0$  at  $t_0 = 0$ .
- c) Do we have induced current  $I_0$ ? Why?
- d) In case the millivoltmeter is replaced by a resistor  $R=5\Omega$ . Find the induced current  $I_0$  at  $t_0 = 0$ , and the electromagnetic force  $\vec{F}_0$  in  $M_0N_0$  at same instant. Is the oscillation of MN in this case damped or undamped? Why? What must we do for MN to produce S.H.M, and what do we call such motion?

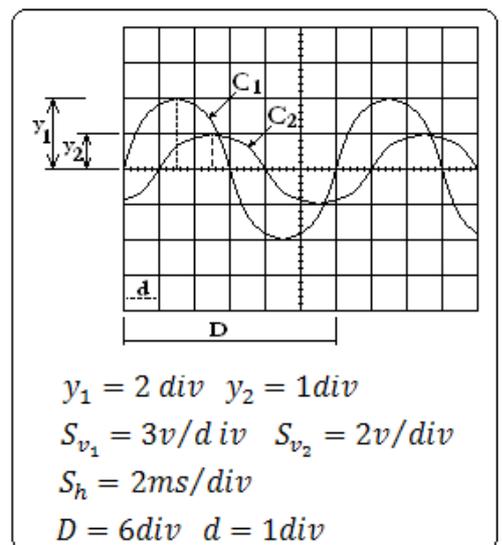
III- Study of sinusoidal alternating current – voltage.....(6pts.)

The adjacent circuit consists of a low frequency generator connected in series to a capacitor, of capacitance  $C= 50\mu F$ , a coil (L,r) and a resistor of resistance  $R= 20\Omega$ .

An oscilloscope is connected to the circuit, to display the voltage  $u_G$  across L.F.G;  $u_R$  across R so we get the curves ( $C_1$ ) and ( $C_2$ ) in the oscillograms.



- 1- a) Calculate the amplitude  $U_{m(1)}$  and  $U_{m(2)}$  of the displayed voltages, then deduce which curve represents  $u_G$  and draw the connections of the circuit to the oscilloscope.
- b) Calculate the amplitude of the current  $I_m$ , the period of  $u_G$ , and the phase angle  $\varphi$  between  $u_G$  and  $i$ , indicating which one leads the other, then deduce  $u_G$  and  $i$  in terms of t
- c) Find the average power across AE of the circuit, then deduce r.



- 2- The frequency of the L.F.G varies, and when  $u_G = 6 \sin(200\pi t)$  or  $f_0 = 100 \text{ Hz}$ , we observe that  $u_G$  and  $u_R$  are in phase. ( $u_G$  in V, t in S)
  - a) What do we call this phenomenon? Calculate the inductance L of the coil.
  - b) Find the new amplitude  $I'_m$  of the current, then deduce the expression of the current  $i'$  in terms of t.
  - c) Determine the expressions of the voltages  $u_{(coil)}$  and  $u_C$  in terms of time. Good work